



TAQQOSLAMALAR .EYLER FUNKSIYASI.

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ABSTRACT

Maqolada Taqqoslamalar ularning xosslari o'rganilgan. Taqqoslamalarni Eylér va Ferma teoremlari orqali o'rganish.

Z-butun sonlar halqasi bo'lib, $m \geq 1$ natural son bo'lsin. Ta'rif. Agar Z halqaga tegishli a va b sonlarni m natural songa bo'lganda hosil bo'lgan qoldiqlar bir xil bo'lsa, yoki a-b ayirma m ga bo'linsa, yoki $a = b + mq$ tenglik o'rinli bo'lsa, u holda a va b sonlar m modul bo'yicha taqqoslanadi deyiladi va $a \equiv b \pmod{m}$ ko'rinishda belgilanadi.

Taqqoslamalar quyidagi xossalarga ega:

1^o. Taqqoslama ekvivalent binar munosabat.

2^o. Bir xil modulli taqqoslamalarni hadma-had qo'shish (ayirish) mumkin. Bu ish n ta $a_1 \equiv b_1 \pmod{m}$, $a_2 \equiv b_2 \pmod{m}$, ..., $a_n \equiv b_n \pmod{m}$ taqqoslamalar uchun ham bajariladi, ya'ni $a_1 \pm a_2 \pm \dots \pm a_n \equiv (b_1 \pm b_2 \pm \dots \pm b_n) \pmod{m}$ taqqoslamani hosil qilamiz.

Natija. Taqqoslamaning bir qismidagi sonni uning ikkinchi qismiga qarama-qarshi ishora bilan o'tkazish mumkin.

Natija. Taqqoslamaning ixtiyoriy qismiga modulga karrali sonni qo'shish mumkin.

3^o. Bir xil modulli taqqoslamalarni hadma-had ko'paytirish mumkin.

Natija. Taqqoslamaning ikki qismini (modulni o'zgartirmay) bir xil natural darajaga ko'tarish mumkin.

4^o. Modulni o'zgartirmagan holda taqqoslamaning ikki qismini bir xil butun songa ko'paytirish mumkin.

5^o. Agar $x \equiv y \pmod{m}$ bo'lsa, u holda ixtiyoriy butun koeffitsientli $f(x) = a_0x^n + a_1x^{n-1} + \dots + a_{n-1}x + a_n$, $f(y) = a_0y^n + a_1y^{n-1} + \dots + a_{n-1}y + a_n$ ko'phadlar uchun $f(x) \equiv f(y) \pmod{m}$ taqqoslama o'rinli bo'ladi.

6^o. Agar bir vaqtda $a_i \equiv b_i \pmod{m} (i = \overline{1, n})$ va $x \equiv y \pmod{m}$ taqqoslamalar o'rinli bo'lsa, u holda

$a_0 x^n + a_1 x^{n-1} + \dots + a_{n-1}x + a_n = b_0 y^n + b_1 y^{n-1} + \dots + b_{n-1} y + b_n \pmod{m}$ taqqoslama o'rinli bo'ladi.

Natija. Taqqoslamada qatnashuvchi qo'shiluvchini o'zi bilan teng qoldikli bo'lgan ikkinchi songa almashtirish mumkin.

7^o. Taqqoslamaning ikki qismini modul bilan o'zaro tub bo'lgan ko'paytuvchiga qisqartirish mumkin.

8^o. Taqqoslamaning ikki qismini va modulini bir xil musbat songa ko'paytirish, taqqoslamaning ikki qismi va moduli umumiy ko'paytuvchiga ega bo'lsa, u xolda bu taqqoslamaning ikki qismi va modulini bu umumiy ko'paytuvchiga bo'lish mumkin.

9^o. Agar taqqoslama bir necha Modul bo'yicha o'rinli bo'lsa, u holda bu taqqoslama shu modullarning eng kichik umumiy bo'linuvchisi bo'yicha ham o'rinli bo'ladi.

10^o. Agar taqqoslama biror m Modul bo'yicha o'rinli bo'lsa, u holda bu takdoslama modulning ixtiyoriy buluvchisi buyicha ham o'rinli bo'ladi.

11^o. Taqqoslamaning bir qismi va modulining EKUB bilan uning ikkinchi qismi va modulining EKUB o'zaro teng bo'ladi.

Barcha butun sonlarni $m \geq 1$ natural songa bo'lganda $0, 1, 2, \dots, m-1$ qoldiqlar hosil bo'ladi. Bunday har bir qoldiqqa butun sonlarning biror sinfi mos keladi.

Ta'rif. m ga bo'linganda r ga teng bir xil qoldiq beradigan butun sonlar to'plami m modul bo'yicha chegirmalar sinflari deyiladi va uni \bar{r} kabi belgilanadi.

Ta'rif. Chegirmalar sinfining ixtiyoriy elementi shu sinfning chegirmasi deyiladi.

Ta'rif. m Modul bo'yicha tuzilgan har bir chegirmalar sinfidan erkinlik bilan bittadan element olib tuzilgan to'plamga m Modul bo'yicha chegirmalarning to'la sistemasi deyiladi.

Sinfning bitta chegirmasi m Modul bilan o'zaro tub bo'lsa, u holda bu sinfning barcha elementlari ham m Modul bilan o'zaro tub bo'ladi.

Ta'rif. m Modul bilan o'zaro tub bo'lgan barcha chegirmalar sinfidan erkinlik bilan bittadan chegirma olib tuzilgan to'plam chegirmalarning m Modul bo'yicha keltirilgan sistemasi deyiladi.

m modul bo'yicha chegirmalarning keltirilgan sistemasidagi elementlar sonini aniqlash uchun Eyler funktsiyasi deb ataluvchi $\varphi(m)$ funktsiyadan foydalanamiz.

Ta'rif. Agar quyidagi ikkita shart bajarilsa, u holda $\varphi(m)$ sonli funktsiya Eyler funktsiyasi deyiladi:

- $\varphi(1)=1$.

- $\varphi(m)$ funktsiya m dan kichik va m bilan o'zaro tub bo'lgan natural sonlar soni.

Ta'rif. Natural sonlar to'plamida aniqlangan f funktsiya uchun $(m; n)=1$ bo'lganda $f(m \cdot n)=f(m) \cdot f(n)$ tenglik bajarilsa, u holda f funktsiyaga mul'tiplikativ funktsiya deyiladi.

Teorema. Eyler funktsiyasi mul'tiplikativ funktsiya bo'ladi. $\varphi(m)$ Eyler funktsiyasini hisoblash formulalari quyidagilardan iborat: m=p tub son bo'lsa, u holda $\varphi(p)=p-1$ bo'ladi.

$$m = r^\alpha \quad (r\text{-tub son, } \alpha\text{-natural son}) \text{ bo'lsa, u holda } \varphi(p^\alpha) = p^{\alpha-1} \cdot (p-1) \text{ bo'ladi.}$$

$$m = p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k} \text{ bo'lsa, u holda}$$

$$\varphi(m) = \varphi(p_1^{\alpha_1} p_2^{\alpha_2} \dots p_k^{\alpha_k}) = m \left(1 - \frac{1}{p_1}\right) \left(1 - \frac{1}{p_2}\right) \dots \left(1 - \frac{1}{p_k}\right)$$

o`ladi.

Eyler teoremasi. Agar $(a; m)=1$ bo`lsa, u holda $a^{\varphi(m)} \equiv 1 \pmod{m}$ taqqoslama o`rinli bo`ladi.

Ferma teoremasi. Agar a son r tub songa bo`linmasa, u holda $a^{p-1} \equiv 1 \pmod{m}$ taqqoslama o`rinli bo`ladi.

Koeffitsientlari butun sonlardan iborat $f(x) = a_0 x^n + a_1 x^{n-1} \dots + a_{n-1} x + a_n$ ko`phad berilgan bo`lsin.

Ta`rif. Ushbu

$$f(x) \equiv 0 \pmod{m} \quad (a_0 \text{ son } m \text{ ga bo`linmaydi, } a_i \in \mathbb{Z}, m \geq 1) \quad (1)$$

ko`rinishdagi taqqoslamani bir noma`lumli n - darajali taqqoslama deyiladi.

Ta`rif. Agar $x=s$ bo`lganda

$$f(c) \equiv 0 \pmod{m} \quad (2)$$

taqqoslama to`g`ri bo`lsa, u holda s son (1) taqqoslamani qanoatlantiradi deyiladi.

Teorema. Agar s son (1) taqqoslamani qanoatlantirsa, u holda \bar{C} chegirmalar sinfiga tegishli ixtiyoriy son ham (1) taqqoslamani qanoatlantiradi.

Ta`rif. Agar s son (1) taqqoslamani qanoatlantirsa, u holda \bar{C} chegirmalar sinfi (1) taqqoslamani echimi deyiladi.

m modul bo`yicha barcha chegirmalar sinfi $\bar{0}, \bar{1}, \bar{2}, \dots, \overline{m-1}$ bo`ladi. Demak, m modulli taqqoslamani qanoatlantiruvchi sonlarni $0, 1, 2, \dots, m-1$ sonlar ichidan qidirish lozim.

Ta`rif. Yechimlari to`plami ustma-ust tushgan taqqoslamalarni teng kuchli taqqoslamalar deyiladi.

Agar (1) taqqoslamani ikki qismiga ixtiyoriy ko`phad qo`shilsa yoki har ikki qismini m Modul bilan o`zaro tub bo`lgan k songa ko`paytirilsa, yoki ikki qismi va modulini k natural songa ko`paytirilsa, u holda hosil bo`lgan taqqoslama berilgan taqqoslamaga teng kuchli bo`ladi.

Ta`rif. Ushbu $ax \equiv b \pmod{m} \quad (a, b \in \mathbb{Z}, \forall m \in \mathbb{N}) \quad (3)$

ko`rinishdagi taqqoslamaga bir noma`lumli birinchi darajali taqqoslama deyiladi.

Teorema. Agar $(a; m)=1$ bo`lsa, u holda (3) taqqoslama yagona echimga ega bo`ladi.

Teorema. Agar $(a; m)=d$ bo`lib, b son d ga bo`linmasa, u holda (3) taqqoslama echimga ega emas.

Teorema. Agar (3) taqqoslamada $(a; m)=d$ bo`lib, b son d ga bo`linsa, u holda (3) taqqoslama soni d ga teng bo`lgan ushbu

$$\bar{\alpha}, \bar{\alpha} + \frac{m}{d}, \dots, \bar{\alpha} + \frac{(d-1)m}{d} \quad (5)$$

echimlarga ega bo`lib, bundagi α echim $\frac{a}{d} x \equiv \frac{b}{a} \pmod{\frac{m}{d}}$ taqqoslamani yagona echimi bo`ladi.

Ta`rif. Agar $f(x) = a_0 x^p + a_1 x^{p-1} + \dots + a_{n-1} x + a_n, a_i \in \mathbb{Z}, r$ -tub son, a_0 con r ga bo`linmasa, u holda ushbu

$$f(x) \equiv 0 \pmod{p} \quad (6)$$

taqqoslamaga tub modulli p -darajali bir noma`lumli taqqoslama deyiladi.

Teorema. Agar (6) taqqoslamada a_0 bosh koeffitsient r ga bo`linmasa, u holda (6) taqqoslama bosh koeffitsienti 1 ga teng bo`lgan boshqa bir taqqoslamaga teng kuchli bo`ladi.

Teorema. Agar $f(x)$ va $g(x)$ koeffitsientlari butun sonlardan iborat ko'phadlar bo'lsa, u holda

$$f(x) \equiv 0 \pmod{p}, \quad (7)$$

$$f(x) - (x^p - x)g(x) \equiv 0 \pmod{p} \quad (8)$$

taqqoslamalar teng kuchli bo'ladi.

Teorema. Darajasi n ($n > r$) bo'lgan r tub modulli taqqoslama darajasi $r-1$ dan katta bo'lmagan taqqoslamaga teng kuchli bo'ladi.

Teorema. Tub modulli n -darajali taqqoslama echimlari soni n tadan ortiq emas.

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